# Stochastic Entry of Enveloped Viruses: Fusion versus Endocytosis

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ABSTRACT Infection by membrane-enveloped viruses requires the binding of receptors on the target cell membrane to glycoproteins, or "spikes," on the viral membrane. The initial entry mechanism is usually classified as fusogenic or endocytotic. However, binding of viral spikes to cell surface receptors not only initiates the viral adhesion and the wrapping process necessary for internalization, but can simultaneously initiate direct fusion with the cell membrane. Both fusion and internalization have been observed to be viable pathways for many viruses. We develop a stochastic model for viral entry that incorporates a competition between receptor-mediated fusion and endocytosis. The relative probabilities of fusion and endocytosis of a virus particle initially nonspecifically adsorbed on the host cell membrane are computed as functions of receptor concentration, binding strength, and number of spikes. We find different parameter regimes where the entry pathway probabilities can be analytically expressed. Experimental tests of our mechanistic hypotheses are proposed and discussed.

#### INTRODUCTION

Viral entry mechanisms are typically classified as either endocytotic, or as fusogenic (1). In the latter, the virus membrane, after association with the surface of the host cell, fuses and becomes contiguous with the cell membrane. This process is mediated by the binding of cell surface receptors to glycoprotein spikes on the viral membrane surface, forming fusion competent complexes spanning the viral and cell membranes. In endocytosis, the host cell first internalizes the virus particle, wrapping it in a vesicle before acidification-induced fusion with the endosomal membrane can occur. Wrapping can occur only after cell surface receptors, which also act as attachment factors, bind to the viral spikes. Experimentally, both fusion with the cell membrane and internalization can be observed and distinguished using microscopy (2,3).

Many viruses, such as influenza and hepatitis B, use endocytosis as their primary mode of entry (4,5). The surface of an influenza virus is coated with  $\sim$ 400 hemagglutinin (HA) protein spikes (6). The HA adheres to sialic acid-containing glycoproteins and lipids on the cell surface leading to wrapping of the virus particle. Particle wrapping may also be mediated by the recruitment of pit-forming clathrin/caveolin compounds (7). Cell membrane pinch-off, leading to internalization of the virus, usually requires additional enzymes such as dynamin and endophilin (8). Endosomal acidification oligomerizes the HA, priming them to fuse with the endosomal membrane. Direct fusion of the influenza virus with the host cell membrane is precluded since HA is activated only in the acidic endosomal environment. However, low pH conditions have also been shown to induce the direct fusion of influenza virus with certain cells (9).

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Recent experiments on the avian leukosis retrovirus have provided evidence both for a pH-dependent direct fusion mechanism (10,11), and an endocytotic pathway (12). Moreover, the entry pathway of some viruses such as Semliki Forest Virus can be shifted from endocytosis to fusion by acid treatment, but only in certain host cell types (13). In this case, low pH triggering of receptor-primed envelope glycoproteins can initiate fusion before the virus can be wrapped and endocytosed. Vaccinia and HIV (typically infecting cells via fusion after association with the cell surface receptor CD4) have also been shown to exploit both entry mechanisms (7,14–16). For example, fusion-independent mechanisms of HIV-1 capture and internalization in mature dendritic cells, mediated by DC-SIGN (17), can be a significant mode of HIV transmission through dendritic cells and lymphatic tissue (18). Capture by DC-SIGN and CLEC-2 adhesion molecules also internalizes HIV in platelets (19). Thus, depending upon physical conditions and cell type, both entry pathways are potentially accessible to certain viruses. The choice seems to depend on the type of receptors the viruses engages, whether they are receptors/coreceptors that induce fusion (perhaps triggered by low pH), or simply attachment factors such as sialic acid-rich glycoproteins that do not induce fusion. In this latter case, complete wrapping before an irreversible fusion event is more likely to occur, and internalization is favored.

It is not surprising that subtle changes in the interactions between viral membrane proteins and cell receptors dramatically affect the infectivity of a virus, as recently demonstrated for the 1918 influenza virus (20). In this article, we model virus-receptor kinetics and propose a mechanism consistent with experimental observations, which describes viral entry by incorporating both fusion and endocytosis entry pathways in a probabilistic manner. In the next section, we develop a stochastic one-species receptor model for the binding of receptors necessary to start the virus wrapping process. These receptors, upon binding, can induce membrane

fusion at each receptor-spike complex. In the Results, we find parameter regimes in which each of the entry mechanisms dominate. Explicit expressions for the entry pathway probabilities, as functions of the relevant kinetic rates, are given in the Appendix. In the Discussion and Summary, we explore the connection between our parameters and experimentally controllable physical conditions such as receptor/coreceptor density, spike density, and cell membrane rigidity. Experimental tests are proposed and extensions of our analysis to more realistically incorporate biological features are discussed.

#### SINGLE SPECIES RECEPTOR MODEL

The basic features of our proposed mechanism are shown in Fig. 1. A virus particle initially nonspecifically adsorbed on the cell membrane (without any bound receptors) can spontaneously dissociate with rate  $k_{\rm d}$ . Alternatively, mobile receptors in the cell membrane can bind specifically to the glycoprotein spikes (assumed here to be uniformly distributed) on the viral surface. Successive addition of receptors to the viral ligands, when n are already attached, occurs with rate  $p_{\rm n}$ . Thus, the binding of the first receptor occurs with rate  $p_{\rm 0}$ . Similarly, desorption of the  $n^{th}$  receptor occurs at rate  $q_{\rm n}$ . We consider the adsorption of a single effective receptor or attachment factor to a spike, lumping together the effects of

multiple receptor/coreceptor types. This approximation is valid when, for example, coreceptor binding is highly cooperative such as suggested in the HIV infection process where CD4 binding to the gp120 protein spike induces rapid CCR5 coreceptor binding (21).

Receptors not only adhere the cell membrane to the viral membrane, but can also initiate local membrane fusion at each receptor-spike complex with rate  $k_{\rm f}$ . Fusion can occur at any time during the receptor recruitment process and is more likely to occur per unit time with more bound receptors. Receptor-spike complexes that are unable to initiate fusion are described by a vanishing fusion rate  $k_f \rightarrow 0$ . However, if receptors have high fusogenicity  $k_f$ , the virus might fuse only after a single receptor has attached. Only if the system reaches a fully wrapped state with N bound receptors (Fig. 1 f), before any fusion event occurs, can pinch-off and endocytosis occur with rate  $k_e$ . The number of spikes N is typically large, varying among viruses such as HIV ( $N \sim 15$ ) (22), SIV ( $N \sim 70$ ) (22), and Influenza ( $N \sim 400$ ) (6). The path to endocytosis is thus a race between fusion and complete wrapping of a relatively large number N of viral spikes.

States in the model are labeled by the index n (Fig. 2), representing the number of formed receptor-spike complexes. Starting from a nonspecifically adsorbed virus particle denoted by state n=0, the system progresses along the chain with the appropriate transition rates corresponding to

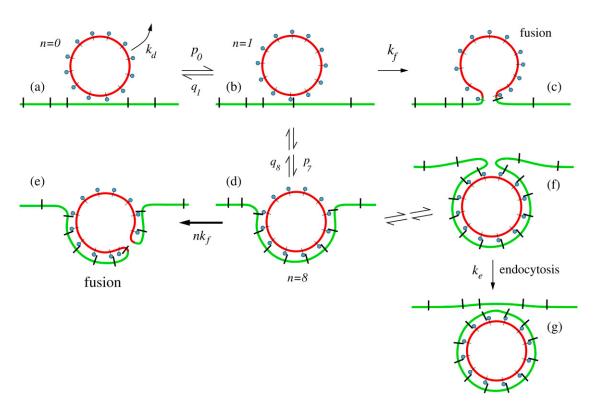


FIGURE 1 A schematic of viral entry pathways. (a) A nonspecifically adsorbed virus particle can desorb with rate  $k_d$ , or it can (b) recruit and specifically bind a receptor. The receptor can immediately initiate membrane fusion with rate  $k_f$  as shown in panel c, or, it can recruit additional receptor molecules, inducing wrapping of the virus particle. From partially wrapped states (d), the virus can at any stage undergo membrane fusion (e), or, it can completely wrap and internalize the virus particle (f and g).

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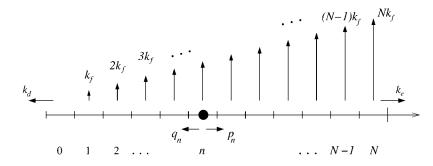


FIGURE 2 The stochastic process representing the competition between membrane fusion and endocytosis. The states n correspond to the number of receptor-spike complexes formed, while N is the total number of spikes on the virus membrane. Each receptor-spike complex can initiate membrane fusion with rate  $k_{\rm f}$ . As more receptors are bound, the total rate of fusion increases linearly. The irreversible pinch-off and endocytosis rate is denoted  $k_{\rm e}$ .

attachment and detachment of cell membrane receptors. The probability  $P_n(t)$  of having n bound receptors (or attachment factors) at time t obeys the master equation

$$\dot{P}_{n}(t) = -(nk_{f} + p_{n} + q_{n})P_{n} + p_{n-1}P_{n-1} 
+ q_{n+1}P_{n+1}, \ 1 \le n \le N - 1, 
\dot{P}_{0}(t) = -(k_{d} + p_{0})P_{0} + q_{1}P_{1}, 
\dot{P}_{N}(t) = -(Nk_{f} + k_{e} + q_{N})P_{N} + p_{N-1}P_{N-1}.$$
(1)

Although we describe the general viral entry process in terms of recruitment and binding of a single type of receptor, our model encompasses processes involving clathrin or caveolin aggregation and pit formation, typically leading to endocytosis. All of these biologically distinct, but physically similar mechanisms can be analyzed by appropriately interpreting the rates. For example, the nucleation of a clathrin-coated pit can be modeled by effective binding and unbinding rates  $p_n$  and  $q_n$  that describe the rates of clathrin addition and removal from the pit. Since individual clathrin molecules are not known to induce membrane fusion, the fusion rate  $k_f=0$ , and only endocytosis (or virus dissociation from the cell surface) would occur. The fusion rate is also negligible if the receptor is a simple attachment factor that causes adherence of the membranes, but does not facilitate fusion.

The receptor binding and unbinding rates,  $p_n$  and  $q_n$ , are related to the cell surface receptor density and the receptorspike binding strength, respectively. The Markov process shown in Fig. 2 implicitly assumes that the receptor recruitment is not diffusion-limited—the rate of addition of successive receptors is independent of the history of previous receptor bindings.

Approximate forms for  $p_n$ ,  $q_n$  can be physically motivated by considering the number of ways additional receptors can bind or unbind, given that n receptor-spike complexes already exist. As the membrane progressively wraps around the virus particle, the rate of addition of the next receptor is proportional to the number  $n_p$  of unattached spikes bordering the virus-cell membrane contact line L, as shown in Fig. 3.

For a large number N of uniformly distributed spikes on a virus particle of radius R, the contact area  $A_{\rm c} \approx 4\pi R^2 n/N \approx 2\pi R^2 (1-\cos\theta_{\rm n})$ , where  $\theta_{\rm n}=\cos^{-1}[1-2n/N]$  is the angle subtended by the contact line when n receptors are attached. Since the area per spike is  $a_{\rm s} \approx 4\pi R^2/N$ , the number of spikes

near the contact perimeter  $L=2\pi R \sin\theta_n$  is found from  $n_{\rm p}\approx L/\sqrt{a_{\rm s}}$ . Upon using the explicit form for  $\theta_{\rm n}$ , we find the number  $n_{\rm p}$  of periphery spikes as a function of  $n\geq 1$  receptor-bound spikes,  $n_{\rm p}\sim\sqrt{\pi N}\sqrt{1-(1-2n/N)^2}$ . At a stage where  $n\geq 1$  receptors have bound,  $\sim n_{\rm p}$  spikes are accessible for additional binding of receptors. Similarly, there are  $\sim n_{\rm p}$  receptor-spike complexes available for dissociation. Combinatorically, the receptor binding and unbinding rates take the form (23)

$$p_{\rm n} \approx p_0 \frac{\sqrt{1 - \left(1 - \frac{2{\rm n}}{\rm N}\right)^2}}{\sqrt{1 - \left(1 - \frac{2}{\rm N}\right)^2}}, \quad q_{\rm n} \approx q_1 \frac{\sqrt{1 - \left(1 - \frac{2{\rm n}}{\rm N}\right)^2}}{\sqrt{1 - \left(1 - \frac{2}{\rm N}\right)^2}}, \quad (2)$$

where  $1 \le n \le N - 1$ ,  $p_0$  is the intrinsic rate of binding the first receptor, and  $q_1 = q_N$  is the dissociation rate of an individual receptor-spike complex. Since  $q_1$  is a spontaneous receptor-spike dissociation rate, it is independent of receptor density and spike number. If the receptor-spike binding energy is at least a few  $k_B T$ , we also expect  $q_n$  to be relatively insensitive to the cell membrane bending rigidity.

A number of physical attributes and biological intermediates can be incorporated into the rate parameters to address more complicated microscopic processes. For example, if thermal fluctuations are rate-limiting, there would be an additional factor in  $p_n$ , reflecting the probability per unit time that a patch of membrane fluctuates to within a distance of the virus surface spike that allows receptor-spike binding. The

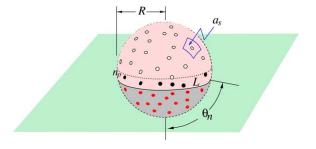


FIGURE 3 Schematic of a partially wrapped virus particle. The unbound spikes above the contact region are represented by open circles, while the receptor-bound spikes in the contact region are represented by the red dots. The number  $n_{\rm p}$  of spikes or spike-receptor complexes near the contact perimeter used to compute  $p_{\rm n}$  or  $q_{\rm n}$  via Eq. 2 are shown as black dots.

dynamics of this process depends on the cell membrane tension and rigidity, the typical spike spacing, and potentially the viscosity of the extracellular environment. For stiff membranes under tension, the wrapping of spherical particles encounters an energy barrier near half-wrapping (24), which can be incorporated into the dynamics by assuming an additional factor in  $p_n$  that has a minimum near  $n \approx N/2$ . Thus, the energy barrier associated with membrane bending will tend to flatten the n-dependence of  $p_n$ .

Particular aspects of the entry process can also influence estimates of the other rates. If the viral spikes are mobile and can aggregate to the initial focal point of adhesion, the target cell membrane is not able to fully wrap and endocytosis is prevented. The overall kinetic scheme remains unchanged except with  $k_{\rm e}\approx 0$ . Finally, the recruitment of secondary coreceptors that occurs in, e.g., HIV fusion, can also be developed within our current framework and is put forth in Discussion and Summary. Although some of the physical details described above influence the specific values of  $p_{\rm n}$ , we will show that for large N, the qualitative behavior of our model can be summarized by distinct parameter regimes, somewhat insensitive to the precise values of  $p_{\rm n}$ ,  $q_{\rm n}$ .

#### **RESULTS**

We solved Eq. 1 for the probabilities  $P_n(t)$  given an initial condition  $P_n(t=0) = \delta_{n,0}$ . Using these probabilities, we find the probability currents through the dissociation, fusion, and endocytosis pathways,  $J_d(t) = k_d P_0(t)$ ,  $J_f(t) = k_f \sum_{n=1}^{N} n P_n(t)$ , and  $J_{\rm e}(t)=k_{\rm e}P_{\rm N}(t)$ , respectively. Fig. 4 shows the current for each pathway as a function of time (in units of  $k_d^{-1}$ ). Note that detachment, fusion, and endocytosis arise sequentially in time. Upon comparing Fig. 4, a and b, we see that changing  $p_{\rm n}$ ,  $q_{\rm n}$  from constant values to the forms in Eq. 2 shifts the currents through the fusion and endocytotic pathways to earlier times. This speedup is simply a consequence of the larger hopping rates  $p_n$ ,  $q_n$ , especially for  $n \approx N/2$ . Nonetheless, the specific form of  $p_n$ ,  $q_n$ , provided they are slowly varying in n, only quantitatively affect the timing of the onset of the currents. The dramatic variations in the infection pathway taken come with changes in  $k_{\rm f}$ . When the fusion rate  $k_{\rm f}$ is increased, endocytosis is suppressed in favor of fusion as shown by Fig. 4, b and c.

Upon time-integrating the currents, we find the total probabilities  $Q_{\rm i}=\int_0^\infty J_{\rm i}(t){\rm d}t, (i=d,e,f)$  for each pathway. Note that from probability conservation,  $Q_{\rm d}+Q_{\rm e}+Q_{\rm f}=1$ . In Fig. 5, we use the binding and unbinding rates given by Eq. 2 to numerically compute the entry pathway probabilities  $Q_{\rm i}$ . Fig. 5 a shows the pathway probabilities as a function of the intrinsic receptor binding rate  $p_0/q_1$ . This ratio is a measure of the density-dependent free energy  $\Delta G$  of the spike-receptor binding:  $p_0/q_1\sim e^{\Delta G/kT}$  (23). In the simplest limit of extremely low receptor density,  $(p_0\to 0)$ ,  $Q_{\rm d}\sim 1-\mathcal{O}(p_0)$ ,  $Q_{\rm f}\sim\mathcal{O}(k_{\rm f}p_0)$ , and  $Q_{\rm e}\sim 0$ , and only dissociation can occur. As  $p_0$  is increased, the probability of fusion increases at the

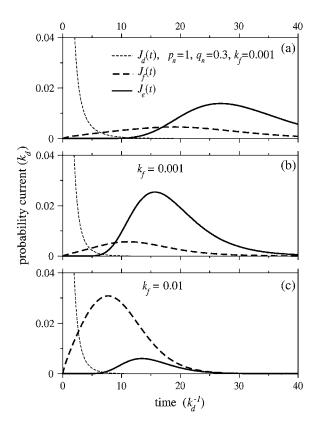
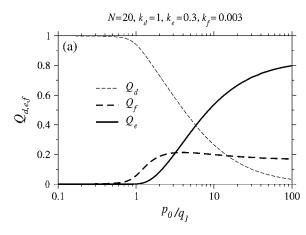


FIGURE 4 The currents through each pathway for N=20 spikes. The thin dashed black curve is the current for desorption, while the thick dashed and solid curves are the currents for fusion and endocytosis, respectively. Time is measured in units of  $k_{\rm d}^{-1}$ , and all rates are normalized with respect to  $k_{\rm d}$ . The parameters used in all plots are  $p_0=1$ ,  $q_1=0.3$ , and  $k_{\rm c}=0.3$ . (a) The currents for constant  $p_{\rm n}=1$ ,  $q_{\rm n}=0.3$ , and fusion rate  $k_{\rm f}=0.001$ . (b) The same parameters except that Eq. 2 is used for the rates  $p_{\rm n}$ ,  $q_{\rm n}$ . (c) The currents with  $p_{\rm n}$ ,  $q_{\rm n}$  as in panel  $p_{\rm r}$ , except that the fusion rate of each spike-receptor complex is increased to  $p_{\rm r}=0.01$ .

expense of desorption. Endocytosis remains negligible, as long the states that occur with any appreciable probability are those with small n. Only as  $p_0 \gg q_1$  does the probability of endocytosis become appreciable and approach the asymptotic expression given by Eq. 3 in the Appendix.

Fig. 5 b shows the total probabilities  $Q_{\rm d}$  of dissociation,  $Q_{\rm f}$  of fusion, and  $Q_{\rm e}$  of endocytosis as functions of the fusion rate  $k_{\rm f}$ . For large detachment rates (e.g.,  $q_1=2>p_0=1$ ),  $Q_{\rm e}\approx 0$ , and fusion can occur only at large  $k_{\rm f}$ , as shown by the thin dotted curve. For the parameters used, N=20,  $p_0=1$ ,  $q_1=k_{\rm e}=0.3$  (normalized by  $k_{\rm d}$ ), the transition from a predominantly endocytotic pathway to a predominantly fusion pathway occurs for  $10^{-3} \leq k_{\rm f} \leq 10^{-2}$ . When  $k_{\rm f} \gg 10^{-2}$ , the sum of fusion probabilities over all intermediate states is appreciable, preventing endocytosis. Therefore, only for a particularly small fusion rate  $k_{\rm f}$ , and nonnegligible endocytosis rate  $k_{\rm e}$ , is internalization possible. We show in the Appendix that generally, if  $p_{\rm n}>q_{\rm n}$ , the effective drift of the stochastic system toward the wrapped state renders the partitioning between fusion and endocytosis controlled by the

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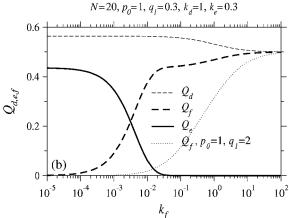


FIGURE 5 Numerical solutions of entry probabilities  $Q_i$  (all rates normalized by  $k_d$ ). (a) The entry probabilities as a function of  $p_0$ . Endocytosis arises only for larger  $p_0 > q_1$ , after the fusion probability becomes significant. Parameters used are N = 20,  $k_f = 0.003$ , and  $k_e = 0.3$  (all rates are normalized by  $k_d$ ). (b) The probabilities of dissociation (thin dashed), fusion (thick dashed), and endocytosis (thick solid) as functions of the individual receptor-spike fusion rate  $k_f$ . Here,  $q_1 = 0.3$ . The thin dotted curve corresponds to a faster receptor detachment rate ( $q_1 = 2$ ), which prevents endocytosis.

fusion rate  $k_{\rm f}$ . If this is the case, the transition from endocytosis to fusion occurs at  $\sim k_{\rm f} (p_{\rm n} + q_{\rm n})/N^2$ , as is confirmed by the numerical solution for N=20 shown in Fig. 5 b.

Although we have chosen N=20 as a representative spike number, different viruses and their variants can have a widely varying number of active spikes. In Fig. 6, we show how the entry pathway probabilities depend on the number N of active viral spikes. As N is increased, the probability for fusion increases at the expense of endocytosis. For  $N \to \infty$  and a nonzero  $k_{\rm f}, Q_{\rm c} \to 0$ , since fusion will likely occur during the infinitely long wrapping processes. For small N, the plotted probabilities must be interpreted with an N-dependent  $k_{\rm e}$ . Suppose  $N \lesssim 10$ . Even if all spikes are receptor-bound, the membrane has an appreciable distance to bend and before full wrapping and endocytosis can occur. Effectively, the fusion rate  $k_{\rm e}$  starts to decrease if N gets small such that the rate of membrane fluctuations over a typical interspike distance decreases.

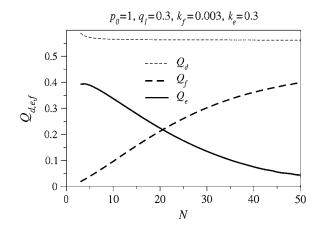


FIGURE 6 The pathway dependence on receptor association/dissociation rates and the number *N* of virus spikes. The number of spikes controls which regime of Eqs. 4 or 5 is valid. Large *N* enhances fusion almost entirely at the expense of endocytosis.

Provided  $p_n - q_n \gg 1/N$ , asymptotic analysis of the solutions reveal qualitatively different behaviors depending upon how the fusion rate  $k_f$  compares with 1/N. If the receptor-spike complex is highly fusion-competent such that  $k_f/(p_n+q_n)\gg 1/N$ , the probability of reaching a completely wrapped  $(n\approx N)$  state is exponentially small and endocytosis cannot occur. Here, the virus pathway is nearly entirely partitioned between dissociation and fusion, as indicated by the asymptotic expressions for  $Q_i$  given by the expressions in Eq. 4.

If  $1/N^2 \ll k_{\rm f}/(p_{\rm n}+q_{\rm n}) \ll 1/N$ , the receptor-spike complex has intermediate fusogenicity. In this case, the time-integrated probability  $\int_0^\infty P_{\rm n}(t) {\rm d}t$  used to construct  $Q_{\rm i}$  remains small for  $n \approx N$  and the probability of endocytosis is still exponentially small, despite the smaller  $k_{\rm f}$ . In this regime, we find an expression for  $Q_{\rm d}$  in Fig. 5. Only when  $k_{\rm f}/(p_{\rm n}+q_{\rm n}) \ll 1/N^2$  is virus internalization appreciable. Expressions for  $Q_{\rm f}$  and  $Q_{\rm e}$  in this very weak fusogenicity limit are also displayed in Eq. 5. The expressions we find agree with the exact numerical evaluation of  $Q_{\rm d,\ e,\ f}$  from solving Eq. 1.

## **DISCUSSION AND SUMMARY**

Fusion can be directly distinguished from endocytosis by imaging fluorescent markers loaded into viruses or model vesicles. Upon fusion, one expects to see an immediate release of marker into the periphery of the target cell. Similarly, single-liposome fluorescence imaging experiments that label and detect vesicle lipids, as they mix with a supported bilayer upon fusion (25), can be used as in vitro model systems for virus fusion. In such experiments, the model parameters  $p_n$ ,  $q_n$ ,  $k_f$ ,  $k_e$ ,  $k_d$  can be tuned by controlling certain physical chemical properties, enabling one to dissect the mechanism of viral entry. The entry pathways delineated by the

different parameter regimes described in the previous section, and by the asymptotic formulae given in the Appendix, provide a framework for analyzing and designing viral entry experiments as well as liposome-based drug delivery protocols.

The receptor density plays the first critical role via the binding rate parameter  $p_n$ . For low receptor densities and proportionately lower  $p_n$  (but fixed spontaneous detachment rate  $q_n$ ), the virus particle can only dissociate or fuse. Although lowering receptor concentration decreases the overall entry probability, it can increase  $Q_f/Q_e$ , the fusion probability relative to endocytosis probability (see Fig. 5 a). Only for  $p_n - q_n > O(1/N)$  can the receptor spike complex fusion rate  $k_f$  become important in determining whether fusion or endocytosis occurs. For endocytosis to occur, the fusion rates must be small such that  $k_f/(p_n + q_n) \ll 1/N^2$ . The rate  $p_n$  can also be substantially decreased by increasing the target membrane surface tension, thereby suppressing the thermal fluctuations of the membrane required to bring cell receptors and viral spikes into proximity.

The rapid drop-off in endocytosis predicted as the fusion rate is increased from  $k_f/(p_n + q_n) \ll 1/N^2$  to  $k_f/(p_n + q_n)$  $\gg 1/N^2$ , especially for large N, shows that tuning physical conditions (such as pH or temperature) that affect the fusogenicity of receptor-spike complexes,  $k_{\rm f}$ , can have a large effect on the viral entry pathway. Recent experiments by Melikyan et al. (26), Henderson and Hope (27), and others have shown a rate-limiting intermediate in the HIV fusion process that can be arrested by lowering temperature. Since CD4 binding was not the rate-limiting step, lowering the temperature decreases  $k_{\rm f}$  to a degree presumably much less that  $(p_n + q_n)/N^2$ , preventing fusion. If these systems have the necessary endocytotic machinery and support pinch-off, lowering temperature and arresting the receptorspike fusion complex while retaining the adhesive wrapping of receptor-spike binding would enhance the endocytotic pathway. The effective rate  $k_{\rm f}$  can also be lowered by crosslinking (with, e.g., defensins) membrane glycoproteins, rendering their complexes with viral spikes fusion-incompetent (28). However, if the cross-linked glycoproteins retain their attraction for the viral surface, the probability of wrapping and internalization would increase. If an independent measurement or estimate of  $p_n + q_n$  is available, the dependence of  $k_f$  on temperature, pH, and chemical modification can be probed. Our results also have implications for fusion inhibitors currently being developed to prevent HIV entry. As shown in Fig. 4, the different timing of fusion versus endocytosis may provide a window for the action of fusion inhibitors. However, our findings suggest that endocytosis can still occur even if fusion is prevented.

Finally, pathways to fusion and endocytosis can diverge for systems that require both primary receptors and secondary receptors (coreceptors). If two species are required, one for adhering cell and viral membranes, and another to induce fusion, endocytosis will be favored, all else being equal. In this case, the initial receptor binding only causes the cell membrane to wrap around the virus particle. An additional coreceptor must diffuse and bind to the spike-receptor adhesion complex to induce fusion. A highly cooperative receptor-coreceptor interaction, such as in HIV fusion involving CD4 and CCR5/CXCR4, is still modeled by Eq. 1, but with the binding rates  $p_n$  interpreted as an effective binding rate for both classes of receptor, proportional to the product of their surface concentrations. However, if the coreceptor density and/or mobility is limiting (16), the binding of receptors occur first, with coreceptor priming and formation of a fusion competent receptor-spike complex occurring slowly. This allows time for receptor (adhesion molecule) mediated membrane wrapping of the entire virus, enhancing the likelihood of endocytosis. Thus, by maintaining a high adhesion receptor density, and lowering the fusion-enabling coreceptor density, one enhances the endocytotic pathway.

## **APPENDIX**

Consider the Master Equation (Eq. 1) in the form  $\dot{\mathbf{P}}(t) = -[\mathbf{M}_0 + \mathbf{M}_f]\mathbf{P}$ , where  $\mathbf{M}_0$  is the conserved random walk transition matrix involving only  $k_d$ ,  $p_n$ ,  $q_n$ , and  $k_e$ , and  $\mathbf{M}_f = k_f \operatorname{diag}(n)$  is a decay term arising from fusion. Large N expressions for the entry pathway probabilities  $Q_i$  can be obtained in different limits

In the limit where the receptor binding is irreversible  $(p_{\rm n}/q_{\rm n}\to\infty)$ , Eq. 1 can be solved exactly:

$$Q_{d} = \frac{k_{d}}{p_{0} + k_{d}}$$

$$Q_{f} = \frac{1}{p_{0} + k_{d}} \left[ p_{0} - \frac{k_{e} p_{N-1}}{k_{e} + N k_{f}} \prod_{m=1}^{N-1} \frac{p_{m-1}}{p_{m} + m k_{f}} \right]$$

$$Q_{e} = \frac{k_{e}}{k_{e} + N k_{f}} \frac{p_{N-1}}{p_{0} + k_{d}} \prod_{j=1}^{N-1} \frac{p_{m-1}}{p_{m} + m k_{f}}.$$
(3)

If  $q_n = 0$ , the probability of dissociation is fixed by  $k_d$  and  $p_0$ , and the remaining current is partitioned between fusion and endocytosis. For a given  $p_0$ ,  $k_f$ ,  $k_e$ , this limit gives the highest probability of the maximally wrapped state and the highest endocytosis probability.

When  $p_n-q_n\gg 1/N$ , there are two possible limits corresponding to high receptor-spike fusion rates,  $k_f/(p_n+q_n)\gg 1/N$ , and intermediate fusion rates  $1/N\gg k_f/(p_n+q_n)\gg 1/N^2$ . For  $k_f/(p_n+q_n)\gg 1/N$ ,  $\int_0^\infty P_n(t)\mathrm{d}t$  is nonnegligible only for  $n\approx 0$  and  $\int_0^\infty P_N(t)\mathrm{d}t$  is exponentially small. A small n local analysis of Eq. 1 yields

$$\begin{split} Q_{\rm d} &\approx \frac{k_{\rm d}}{k_{\rm d} + p_0 - p_0 q_1 / (p_1 + q_1)} \\ Q_{\rm f} &\approx \frac{p_0}{k_{\rm d} + p_0 + k_{\rm d} q_1 / p_1}, \quad \text{and} \\ Q_{\rm e} &\approx 0, \quad \text{for} \quad \frac{k_{\rm f}}{p_{\rm n} + q_{\rm n}} \gg 1/N, \end{split} \tag{4}$$

explicitly showing the absence of endocytosis. The values for  $Q_{\rm d}$  and  $Q_{\rm f}$  corresponding to the parameter values used in Fig. 6 are  $Q_{\rm d}\approx 0.56$  and  $Q_{\rm f}\approx 0.435$ , which agree well with the large N limit of the numerical solution.

In an intermediate fusogenicity regime,  $1/N \gg k_f/(p_n + q_n) \gg 1/N^2$ ,  $\int_0^\infty P_n(t) dt$  is nearly constant for  $n \ll N$ . However,  $\int_0^\infty P_N(t) dt$  remains

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small and endocytosis, although still unlikely, occurs with slightly higher probability than in the high fusogenicity limit. In this intermediate limit, one might first attempt perturbation theory for  $k_f = 0$  (since its largest element of  $\mathbf{M}_{\rm f}$ ,  $Nk_{\rm f} \ll p_{\rm n} + q_{\rm n}$ , is much smaller than the typical elements of  $\mathbf{M}_{\rm 0}$ ). However, as 1/N decreases, so do the spacings between eigenvalues of the zero-fusion transition matrix  $M_0$ . Heuristically, for perturbation theory to be accurate for slowly varying  $p_{\rm N},\,q_{\rm N},$  the largest of the diagonal correction terms,  $Nk_f$ , must be smaller than  $(p_n + q_n)/N$ , the typical spacing between eigenvalues. First-order perturbation for all  $P_n(t)$  is accurate only if  $k_{\rm f}/(p_{\rm n}+q_{\rm n})\ll 1/N^2$ , as is explicitly shown by Eq. 3. Upon expanding  $Q_{\rm f}$  and  $Q_{\rm e}$  (from Eq. 3) in powers of  $k_{\rm f}$ , one finds  $O(N^2)$  corrections terms. Thus, the expansion is only accurate if  $k_{\rm f}/(p_{\rm n}+q_{\rm n})\ll 1/N^2$ . Endocytosis is preempted by fusion or dissociation only when perturbation theory about a nonnegligible  $Q_{\rm e}$  fails (when  $k_{\rm f}/(p_{\rm n}+q_{\rm n})\ll 1/N^2$ ). Perturbation results, for the few-receptor states  $n \approx 0$  important for the dissociation probability  $Q_d$ , are still valid as long as  $k_f/(p_n+q_n) \ll 1/N$ . However, the perturbation results that include the flux through larger  $(n \approx N)$  states are accurate only if the receptor-spike complexes are extremely inefficient at initiating membrane fusion, and  $k_{\rm f}/(p_{\rm n}+q_{\rm n})\ll 1/N^2$ . Thus, for small enough  $k_{\rm f}/(p_{\rm n}+q_{\rm n})$ , we find

independent of  $k_{\rm f}$ . Equations 3–5 give estimates for the entry probabilities  $Q_{\rm d,e,f}$  in the different parameter regimes. For small N such that  $k_{\rm f}/(p_{\rm n}+q_{\rm n})\ll N^{-2},~Q_{\rm e}\approx 0.411,$  which agrees well with the limit shown in Fig. 6.

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